

# Scientifically-Interpretable Reasoning Network (SciReN): Uncovering Hidden Relationships in the Soil Carbon Cycle

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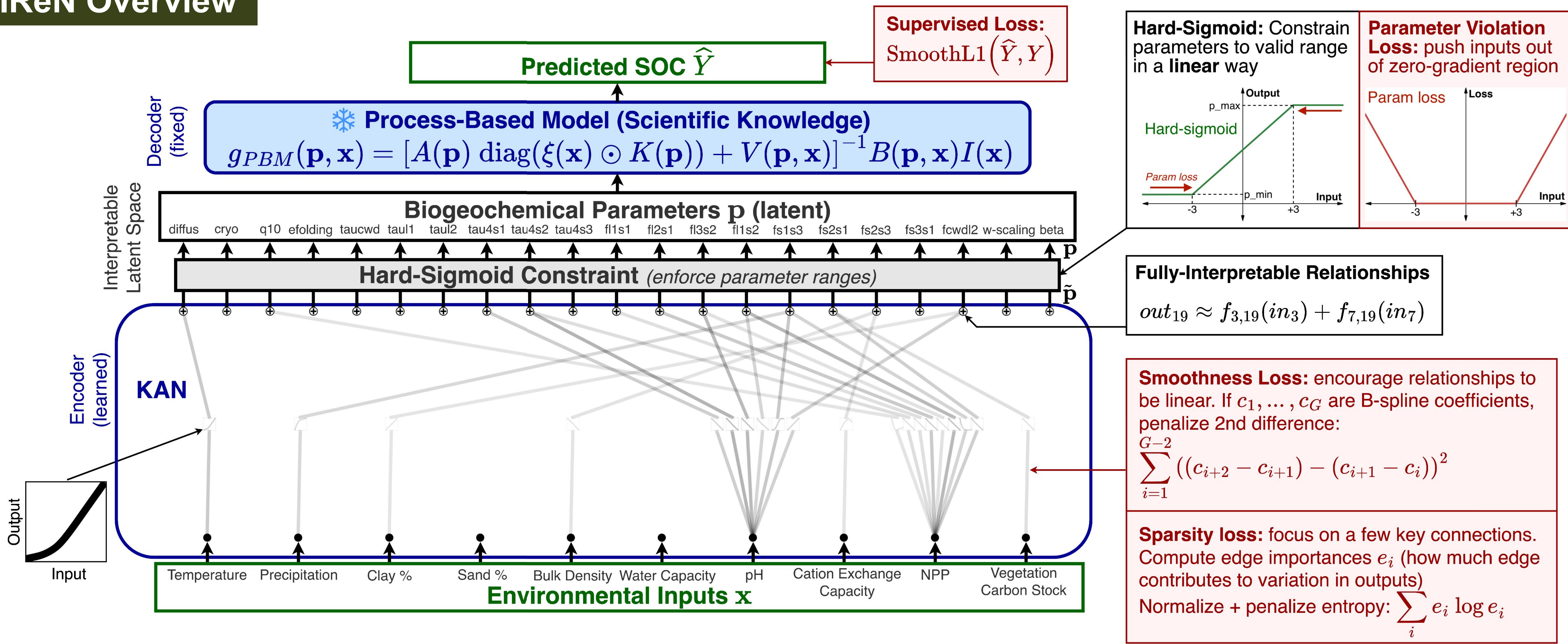
## Motivation

- Soils store vast amounts of carbon (more than atmosphere+plants) [1]
  - Potential to remove CO<sub>2</sub> from the atmosphere, mitigate climate change
- However, the **soil carbon cycle** remains poorly understood, leading to major uncertainties in climate projections [2]
  - e.g. How much carbon is currently stored in the soil? How long does it stay there?
- Scientists encode their scientific understanding into **process-based models** that simulate how carbon moves through the soil
  - Many unknown parameters that vary across space :(

## Approach

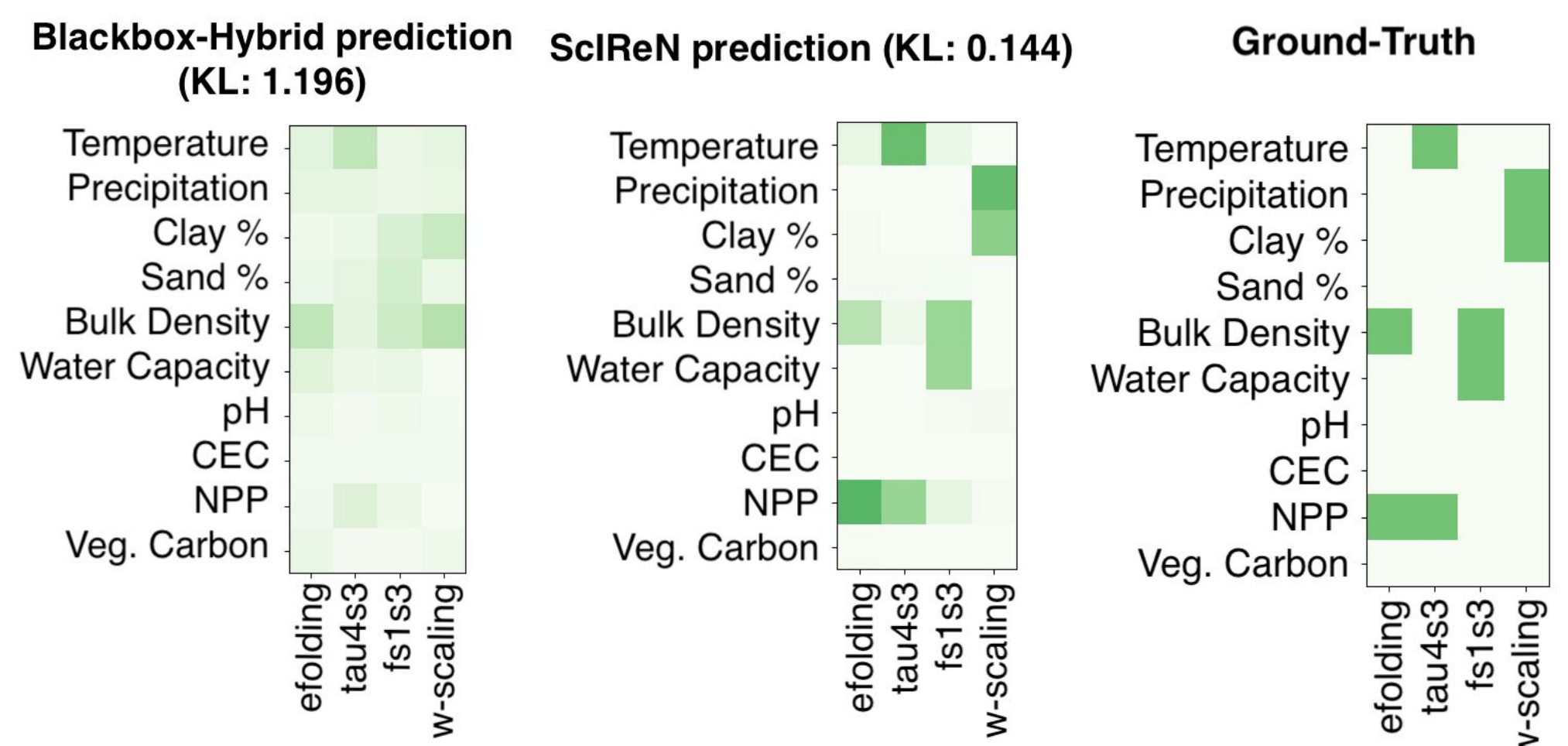
- Idea: embed differentiable process-based model inside neural network [3]
- Encoder**: Given environmental features, predict latent parameters
- Process-based “decoder”**: given predicted parameters, uses **scientific knowledge** to simulate carbon flows and predict carbon amount in each pool
- However, the encoder is **not interpretable**
  - Scientists want **functional relationships** between inputs and parameters
  - Idea: use sparse Kolmogorov-Arnold network [4][5]
- We propose **Scientifically-Interpretable Reasoning Network (SciReN)**, a transparent model that **respects existing knowledge** and **reveals new insights**

## SciReN Overview



## Functional Relationships

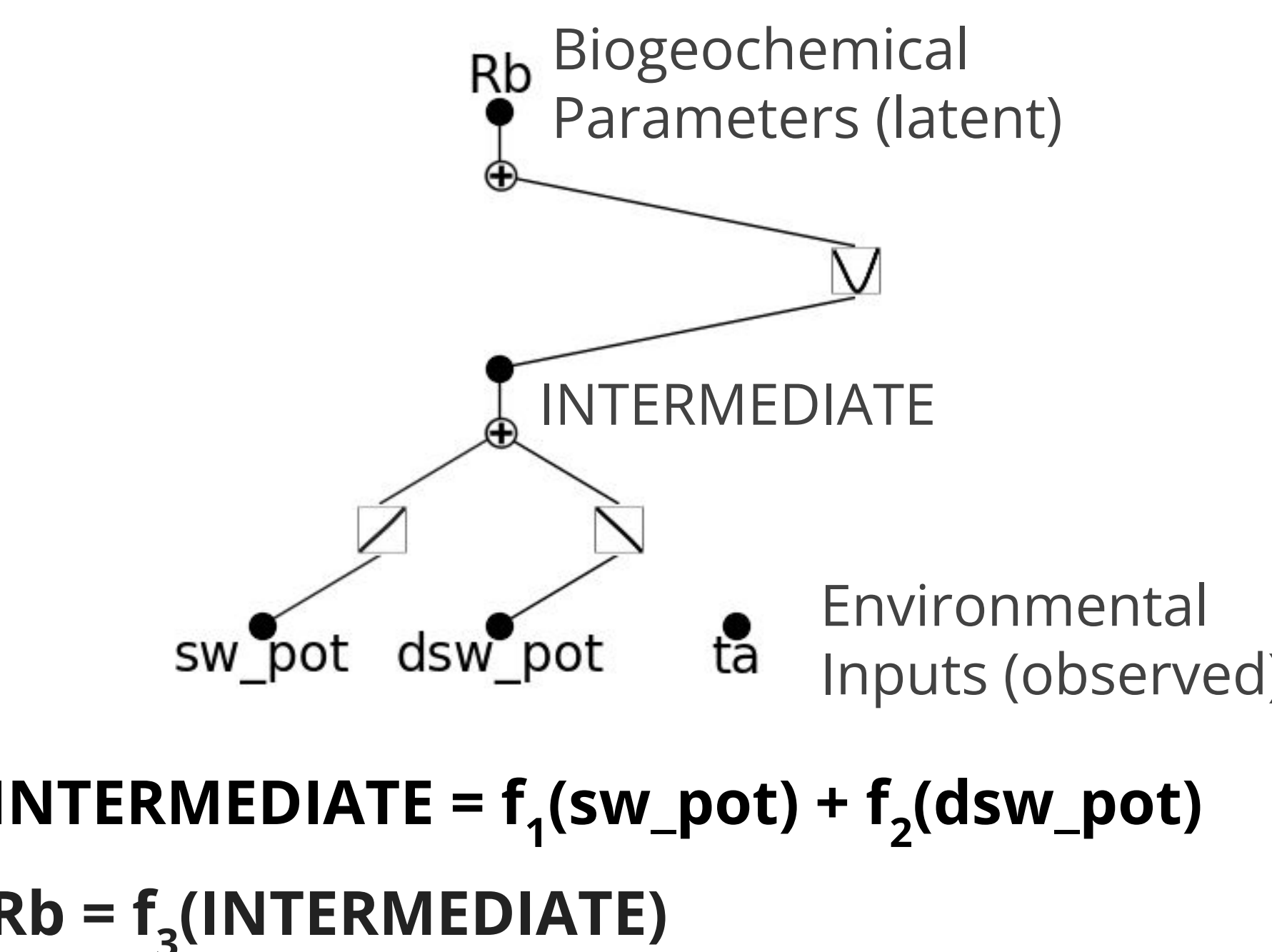
- Each curve reveals how changing one environmental variable will affect a biogeochemical process
- Each output is the sum of interpretable contributions from each input, e.g.
  - output1 = (input1)<sup>2</sup> + exp(input6) + ...**
- How accurate are these? Prescribed functional relationships between 10 inputs and 4 most sensitive biogeochemical parameters (right)



- BINN (left) does not reveal functional relationships. If we apply a post-hoc interpretation method, it did not even implicitly learn the correct relationships.
- SciReN (center) revealed the relationships accurately. **(Also worked on a different domain)**

## Going deeper

If we need non-additive feature interactions, try multi-layer KANs! Example:



## Results

**Synthetic labels:** SciReN is by far the best at recovering latent parameters and functional relationships, and extrapolating out-of-distribution (see paper for more)

Method	$R^2$ (observed, $\uparrow$ )	$R^2$ (latent, $\uparrow$ )	KL, functional relationships ( $\downarrow$ )
Pure-NN	$0.933 \pm 0.015$	N/A	N/A
Blackbox-Hybrid, nonlinear constraint	$0.996 \pm 0.003$	$0.226 \pm 0.800$	$1.312 \pm 0.170$
Blackbox-Hybrid, linear constraint	$0.995 \pm 0.003$	$0.721 \pm 0.226$	$1.082 \pm 0.258$
Linear-Hybrid, hardsigmoid	$0.973 \pm 0.013$	$0.087 \pm 1.014$	$1.727 \pm 0.322$
SciReN, linear constraint (1-layer KAN)	$0.999 \pm 0.002$	$0.989 \pm 0.020$	$0.080 \pm 0.042$

**Real labels:** With SciReN, we get **interpretability without sacrificing accuracy**. While we don't have ground-truth for latent params/relationships, they match domain knowledge.

Method	$R^2$ ( $\uparrow$ )	MAE ( $\downarrow$ )	Pearson correlation ( $\uparrow$ )
Pure-NN	$0.552 \pm 0.173$	$4609.3 \pm 356.8$	$0.780 \pm 0.053$
Blackbox-Hybrid, nonlinear constraint	$0.584 \pm 0.082$	$4726.2 \pm 727.3$	$0.776 \pm 0.048$
Blackbox-Hybrid, linear constraint	$0.589 \pm 0.070$	$4849.7 \pm 650.3$	$0.774 \pm 0.040$
Linear-Hybrid, hardsigmoid	$0.552 \pm 0.082$	$4984.8 \pm 771.6$	$0.761 \pm 0.046$
SciReN, linear constraint (1-layer KAN)	$0.582 \pm 0.080$	$4708.2 \pm 673.1$	$0.769 \pm 0.049$
SciReN, linear constraint (2-layer KAN)	$0.571 \pm 0.094$	$4707.3 \pm 826.3$	$0.765 \pm 0.052$

## Conclusion

We propose SciReN, a method that

- Respects existing scientific knowledge**, provided by any process-based model
- Reveals new functional relationships** between environmental inputs and **unobserved biogeochemical processes**

The system is trainable end-to-end; every part of the model is **fully transparent**.

**Potential future directions:**

- Apply SciReN to new domains
- Experimentally validate the functional relationships learned by the model
- Make SciReN easier to train
- Understand **uncertainty** of revealed functional relationships
- Improve spatial generalization, e.g. geographic positional embeddings or domain adaptation

## References

- [1] Jobbagy, E. G.; and Jackson, R. B. 2000. The vertical distribution of soil organic carbon and its relation to climate and vegetation. *Ecological applications*, 10(2): 423–436.
- [2] Luo, Y., Ahlström, A., Allison, S. D., Batjes, N. H., Brovkin, V., Carvalhais, N., ... & Zhou, T. (2016). Toward more realistic projections of soil carbon dynamics by Earth system models. *Global Biogeochemical Cycles*, 30(1), 40–56.
- [3] Xu, H., Fan, J., Tao, F., Jiang, L., You, F., Houlton, B. Z., ... & Luo, Y. (2025). Biogeochemistry-Informed Neural Network (BINN) for Improving Accuracy of Model Prediction and Scientific Understanding of Soil Organic Carbon. arXiv preprint arXiv:2502.00672. **Submitted to Geoscientific Model Development.**
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